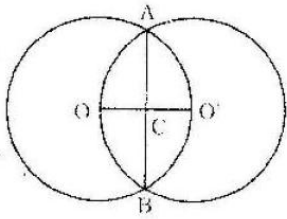


## Simple Circle and Tangent Solution

|   |   |    |   |    |   |    |   |    |   |    |   |
|---|---|----|---|----|---|----|---|----|---|----|---|
| 1 | B | 9  | b | 17 | b | 25 | d | 33 | C | 41 | B |
| 2 | B | 10 | A | 18 | a | 26 | c | 34 | D | 42 | B |
| 3 | a | 11 | C | 19 | b | 27 | B | 35 | B | 43 | C |
| 4 | a | 12 | d | 20 | d | 28 | c | 36 | A | 44 | d |
| 5 | D | 13 | B | 21 | A | 29 | b | 37 | D | 45 | c |
| 6 | A | 14 | a | 22 | * | 30 | b | 38 | d |    |   |
| 7 | B | 15 | b | 23 | a | 31 | B | 39 | C |    |   |
| 8 | * | 16 | d | 24 | d | 32 | * | 40 | B |    |   |

1.



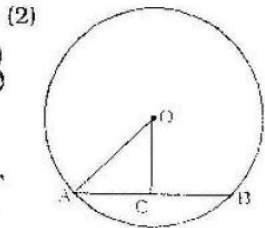
$OC = 2\text{ cm}$   
 $OA = 4\text{ cm}$

$$\therefore AC = \sqrt{4^2 - 2^2} = \sqrt{16 - 4}$$

$$= \sqrt{12} = 2\sqrt{3}$$

$$\therefore AB = 4\sqrt{3}\text{ cm}$$

2.



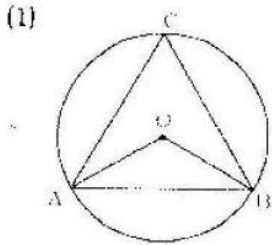
$AC = CB = 4\text{ cm}$   
 $OC = 3\text{ cm}$

$$\therefore OA = \sqrt{OC^2 + CA^2}$$

$$= \sqrt{3^2 + 4^2}$$

$$= \sqrt{9 + 16} = \sqrt{25} = 5\text{ cm}$$

3.



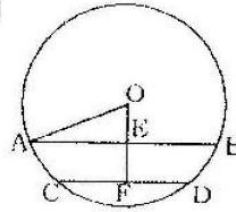
$AO = OB = AB$

$$\therefore \angle AOB = 60^\circ$$

$$\therefore \angle ACB = 30^\circ$$

4.

(1)



Let  $OE = x\text{ cm}$

$$\therefore OF = (x+1)\text{ cm}$$

$$OA = OC = r\text{ cm}$$

$$AE = 4\text{ cm}; CF = 3\text{ cm}$$

From  $\triangle OAE$ ,

$$OA^2 = AE^2 + OE^2$$

$$\Rightarrow r^2 = 16 + x^2$$

$$\Rightarrow x^2 = r^2 - 16$$

From  $\triangle OCF$ ,

$$(x+1)^2 = r^2 - 9$$

By equation (ii) - (i),

$$(x+1)^2 - x^2 = r^2 - 9 - (r^2 - 16)$$

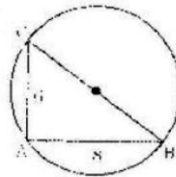
$$\Rightarrow 2x + 1 = 7 \Rightarrow x = 3$$

$\therefore$  From equation (i),

$$9 = r^2 - 16 \Rightarrow r^2 = 25$$

$$\Rightarrow r = 5$$

5.



$$\angle BAC = 90^\circ$$

$\therefore BC$  is the diameter of the circle.

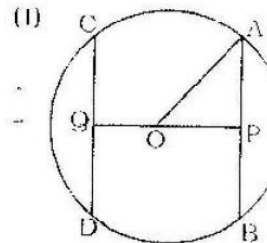
$$\therefore BC = \sqrt{AB^2 + AC^2}$$

$$= \sqrt{8^2 + 6^2} = \sqrt{64 + 36}$$

$$= \sqrt{100} = 10\text{ cm}$$

So that Radius of the circle = 5.

6.



$$AB = CD$$

$$OP = OQ$$

From  $\triangle OAP$ ,

$$OP = \sqrt{OA^2 - AP^2} = \sqrt{5^2 - 4^2}$$

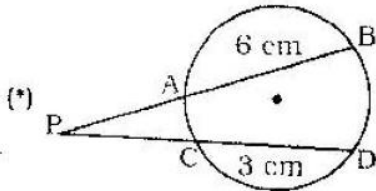
$$= \sqrt{25 - 16}$$

$$= \sqrt{9} = 3\text{ cm.}$$

$$\therefore QP = 2 \times OP = 6\text{ cm.}$$

7. (B) The largest chord of a circle is its diameter.

8. (\*)



$AB = 6 \text{ cm}; CD = 3 \text{ cm}$

$PD = 5 \text{ cm}; PB = ?$

$PA \times PB = PC \times PD$

$\Rightarrow (PB - 6) PB = 2 \times 5$

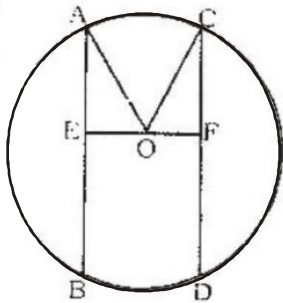
$\Rightarrow PB^2 - 6PB - 10 = 0$

$\Rightarrow PB = \frac{6 \pm \sqrt{36 + 40}}{2}$

$= \frac{6 \pm \sqrt{76}}{2}$

$= \frac{6 + 8.7}{2} \approx 7.35$

9. (b)



$AB = 24$   
 $AE = EB = 12 \text{ cm}$

$OE = \sqrt{OA^2 - AE^2}$

$= \sqrt{15^2 - 12^2}$

$= \sqrt{225 - 144} = \sqrt{81}$

$= 9 \text{ cm}$

$\therefore OF = 21 - 9 = 12 \text{ cm}$

$\therefore CF = \sqrt{15^2 - 12^2} = 9 \text{ cm}$

$\therefore CD = 2 \times 9 = 18 \text{ cm}$

10. (A)

$OE \perp AB$  and  $OF \perp CD$

$AE = EB = 5 \text{ cm}$

$CF = FD = 12 \text{ cm}$

$AO = OC = 13 \text{ cm}$

$AO = OC = 13 \text{ cm}$

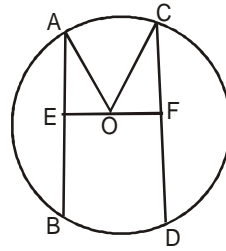
From  $\triangle AOE$

$OE = \sqrt{13^2 - 5^2} = \sqrt{169 - 25} = \sqrt{144} = 12$

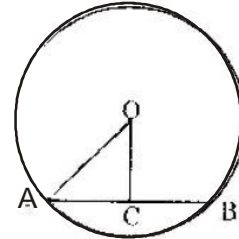
From  $\triangle COF$

$OF = \sqrt{13^2 - 12^2} = \sqrt{25} = 5$

$EF = OE + OF = 17 \text{ cm}$



11. (c)



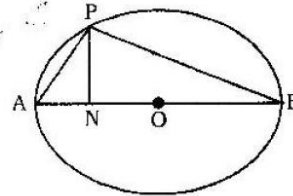
$OC = BC = 4 \text{ cm}$

$AC = 3 \text{ cm}$

$\therefore OC = \sqrt{AC^2 + OC^2}$

$= \sqrt{16 + 9} = \sqrt{25} = 5 \text{ cm}$

12. (d)



$AB = 14 \text{ cm}, PB = 12 \text{ cm}$

$\angle APB = 90^\circ$

$\therefore AP = \sqrt{14^2 - 12^2}$

$= \sqrt{(14 + 12)(14 - 12)}$

$= \sqrt{26 \times 2} = \sqrt{52}$

$ON = x \therefore AN = 7 - x; BN = 7 + x$

$\therefore$  From  $\triangle PAN$ ,  $PN^2 = AP^2 - AN^2$

$= 52 - (7 - x)^2$

$\therefore$  From  $\triangle PNB$ ,

$PN^2 = (12)^2 - (7 + x)^2$

$\therefore 52 - (7 - x)^2 = 144 - (7 + x)^2$

$\Rightarrow 52 - (49 - 14x + x^2) = 144 - (49 + 14x + x^2)$

$\Rightarrow 52 - 49 + 14x - x^2 = 144 - 49 - 14x - x^2$

$\Rightarrow 28x = 144 - 52 = 92$

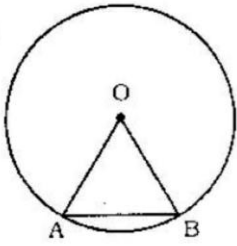
$\Rightarrow x = \frac{92}{28} = \frac{23}{7}$

$\therefore BN = 7 + x$

$= 7 + \frac{23}{7} = \frac{49 + 23}{7} = \frac{72}{7}$

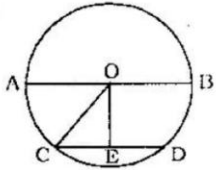
$= 10\frac{2}{7} \text{ cm}$

13. (b)



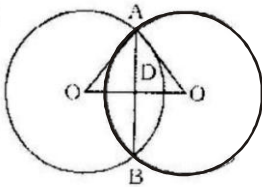
$OA = OB = AB$   
 $\therefore \Delta OAB$  is an equilateral triangle.  
 $\therefore \angle AOB = 60^\circ$

14. (a)



$OC = \text{radius} = 10 \text{ cm}$   
 $CE = ED = 6 \text{ cm}$   
 $\therefore OE = \sqrt{OC^2 - CE^2}$   
 $= \sqrt{10^2 - 6^2} = \sqrt{100 - 36}$   
 $= \sqrt{64} = 8 \text{ cm}$

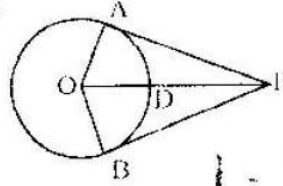
15. (b)



$CD = \sqrt{15^2 - 12^2}$   
 $= \sqrt{225 - 144}$   
 $= \sqrt{81} = 9$   
 $OD = \sqrt{13^2 - 12^2}$   
 $= \sqrt{169 - 144} = \sqrt{25} = 5$   
 $\therefore O'D = 9 + 5 = 14 \text{ cm}$   
 $\angle = 72^\circ = 72 \times \frac{\pi}{180} \text{ radians}$

16.

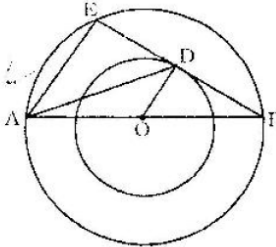
(4)



$OA = OB = r$   
 $OP = 2r$   
 $AP = PB$   
 $= \sqrt{4r^2 - r^2} = \sqrt{3}r$   
 $\sin APO = \frac{OA}{OP} = \frac{r}{2r} = \frac{1}{2}$   
 $\angle APO = 30^\circ$   
 $\therefore \angle APB = 60^\circ$

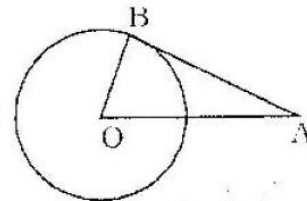
17. (b)

(2)



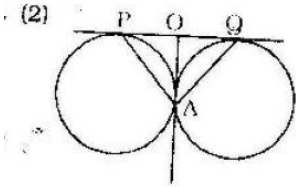
$\angle ODB = 90^\circ$   
 $OD = 8 \text{ cm}$   
 $OB = 13 \text{ cm}$   
 $\therefore BD = \sqrt{13^2 - 8^2}$   
 $= \sqrt{169 - 64}$   
 $= \sqrt{105} \text{ cm}$   
 $AE = 16 \text{ cm}; \angle AED = 90^\circ$   
 $AD = \sqrt{AE^2 + DE^2}$   
 $AD = \sqrt{256 + 105} = \sqrt{361}$   
 $= 19 \text{ cm}$

18.

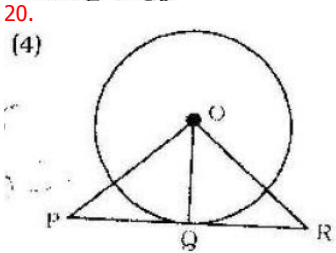


$\angle OBA = 90^\circ$   
 $OA = 5, \quad OB = 4$   
 $\therefore AB = \sqrt{OA^2 - OB^2}$   
 $= \sqrt{25 - 16} = \sqrt{9} = 3 \text{ cm}$

19.



$\Delta O$  is perpendicular to  $PQ$ .  
 $OA = OP = OQ$ .  
 $\angle OPA = \angle OAP = \angle OQA = 45^\circ$   
 $\therefore \angle PAQ = 90^\circ$

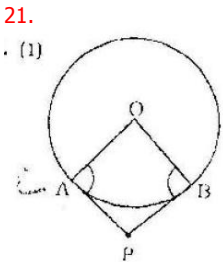


$$QR = \sqrt{OR^2 - OQ^2}$$

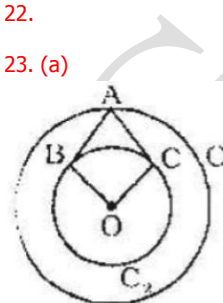
$$= \sqrt{5^2 - 4^2} = 3$$

$$= \sqrt{9} = 3 \text{ cm}$$

$$\therefore PR = PQ + QR = \frac{16}{3} + 3 = \frac{25}{3}$$



$\angle OAP = \angle OBP = 90^\circ$   
 $\angle AOB + \angle APB = 180^\circ$   
 $\Rightarrow 5\angle APB + \angle APB = 180^\circ$   
 $\Rightarrow 6\angle APB = 180^\circ$   
 $\Rightarrow \angle APB = 30^\circ$

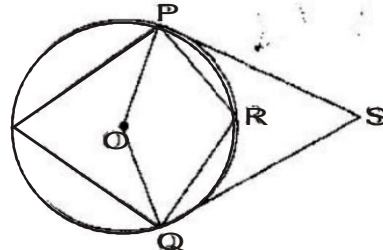


$AB = AC = \text{tangents from the same point}$   
 $OB = OC = 3 \text{ cm}$   
 $OA = 12 \text{ cm}$   
 $\angle ABO = 90^\circ$   
 so that  $AB = \sqrt{12^2 - 3^2} = \sqrt{15 \times 9} = 3\sqrt{15}$

$$\Delta OAB = \frac{1}{2} OB \times AB$$

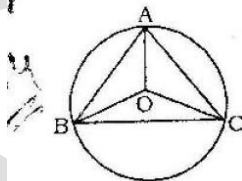
$$= \frac{1}{2} \times 3 \times 3\sqrt{15} = \frac{9\sqrt{15}}{2}$$

so that Area of  $OABC = 9\sqrt{15} \text{ sq.cm.}$   
 24. (d)

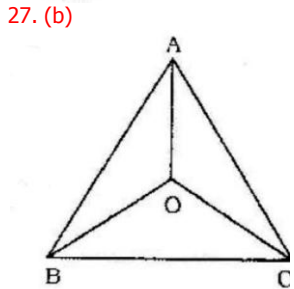


$\angle OPS = \angle OQS = 90^\circ$   
 $\angle PSQ = 20^\circ$   
 $\angle POQ = 160^\circ$   
 $\angle PTQ = 80^\circ$   
 $\therefore QT$  is a concyclic quadrilateral.  
 $\angle PRQ = 180^\circ - 80^\circ = 100^\circ$

25. (d)  
 26.  
 (3)  $\therefore \angle BAC = 85^\circ$   
 $\angle BOC = 2 \times 85^\circ = 170^\circ$

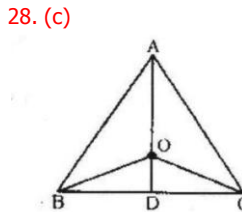


$\therefore \angle OBC = \angle OCB = 5^\circ$   
 $\therefore \angle OCA = \angle OAC = 75^\circ - 5^\circ = 70^\circ$



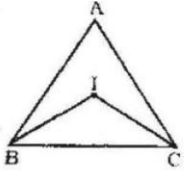
$$\angle BOC = 90^\circ + \frac{1}{2} \angle BAC$$

$$= 90^\circ + 15^\circ = 105^\circ$$



$BO$  is the internal bisector of  $\angle B$   
 $\angle ODB = 90^\circ$ ;  $\angle BOD = 15^\circ$   
 $\angle OBD = 180^\circ - 90^\circ - 15^\circ = 75^\circ$   
 $\angle ABC = 2 \times 75^\circ = 150^\circ$

29. (b)



$$\angle IBC = \frac{1}{2} \angle ABC = 30^\circ$$

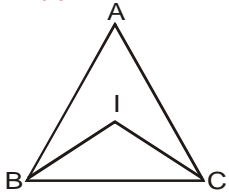
$$\angle ICB = \frac{1}{2} \angle ACB = 25^\circ$$

$$\therefore \angle BIC = 180^\circ - 30^\circ - 25^\circ = 125^\circ$$

30. (b) In radius = side /  $2\sqrt{3}$

$$3 = \frac{\text{side}}{2\sqrt{3}} \Rightarrow \text{side} = 3 \times 2\sqrt{3} = 6\sqrt{3}$$

31. (B)

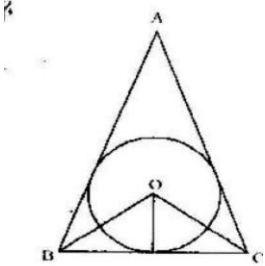


$$\angle IBC = \frac{1}{2} \angle ABC = 65^\circ / 2 = 32.5^\circ$$

$$\angle ICB = \frac{1}{2} \angle ACB = 55^\circ / 2 = 27.5^\circ$$

$$\therefore \angle BIC = 180^\circ - 32.5^\circ - 27.5^\circ = 120^\circ$$

32.



$$\angle BOC = 90^\circ + \frac{A}{2}$$

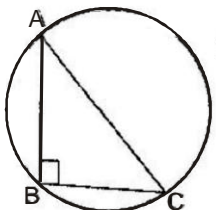
$$\Rightarrow 110 = 90^\circ + \frac{A}{2}$$

$$\Rightarrow A = 2 \times 20 = 40^\circ$$

33. (c) The right bisectors of sides meet at a point called circumcentre.

34. (d) In an equilateral triangle centroid, incentre etc. ie at the same point.

35. (b)



$$3^2 + 4^2 = 5^2$$

triangle ABC is a right angled triangle.

$\angle ABC = 90^\circ =$  angle at the circumference  
diameter of circle = 5 cm  
circum radius = 2.5

36. (a)

OA = OB = OC

$\angle BID = \angle ABC$

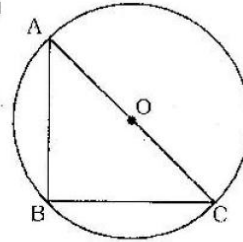
$\Rightarrow x = y$

$\angle BOD = 2 \angle BAD$

$$\therefore \frac{z+x}{y} = \frac{3y}{y} = 3$$

37.

(4)



$$AC = \sqrt{AB^2 + BC^2}$$

$$= \sqrt{15^2 + 20^2} = \sqrt{225 + 400}$$

$$= \sqrt{625} = 25 \text{ cm.}$$

$\angle ABC = 90^\circ$

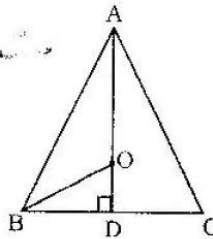
$\therefore AC =$  diameter

$$\therefore \text{Circum radius (OA)} = \frac{25}{2}$$

$$= 12.5 \text{ cm.}$$

38. (d)

(4)



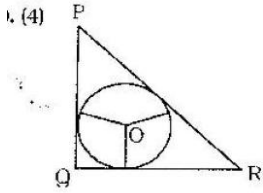
Circum-radius of equilateral triangle

$$\text{gle} = \frac{2}{3} \times \text{height}$$

$$\therefore 8 = \frac{2}{3} \times \text{height}$$

$$\therefore \text{Height} = \frac{8 \times 3}{2} = 12 \text{ cm.}$$

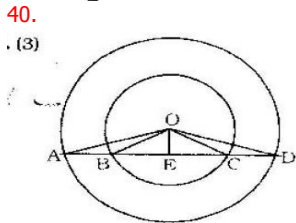
39.



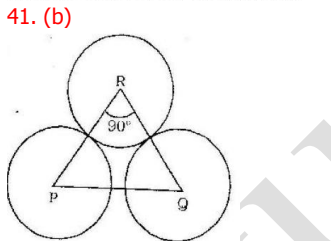
$$\begin{aligned} PR^2 &= PQ^2 + QR^2 \\ &= 3^2 + 4^2 = 25 \\ \therefore PR &= \sqrt{25} \\ &= 5 \text{ cm} \end{aligned}$$

$$r = \frac{\text{Area of triangle}}{\text{Semi-perimeter of triangle}}$$

$$\begin{aligned} &= \frac{\frac{1}{2} \times 3 \times 4}{\frac{3+4+5}{2}} = \frac{6}{6} = 1 \text{ cm} \end{aligned}$$

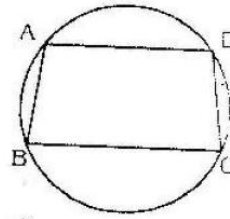


$$\begin{aligned} BE &= EC = 6 \text{ cm}, OB = 10 \text{ cm}, \\ OA &= 17 \text{ cm} \\ \text{From } \triangle OBE, \\ OE &= \sqrt{OB^2 - BE^2} \\ &= \sqrt{10^2 - 6^2} = \sqrt{16 \times 4} = 8 \text{ cm} \\ \text{From } \triangle OAE, \\ AE &= \sqrt{OA^2 - OE^2} \\ &= \sqrt{17^2 - 8^2} = \sqrt{25 \times 9} = 15 \text{ cm} \\ \therefore AD &= 2AE = 2 \times 15 = 30 \text{ cm} \end{aligned}$$



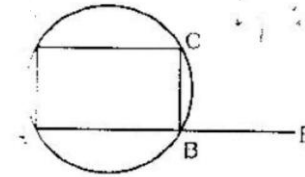
$$\begin{aligned} \angle PRQ &= 90^\circ \\ PR &= 2 + x \\ PQ &= 17 \\ RQ &= 9 + x \\ \therefore PQ^2 &= PR^2 + RQ^2 \\ \Rightarrow 17^2 &= (2+x)^2 + (9+x)^2 \\ \Rightarrow 289 &= 4 + 4x + x^2 + 81 + 18x + x^2 \\ \Rightarrow 289 &= 2x^2 + 22x + 85 \\ \Rightarrow 2x^2 + 22x + 85 - 289 &= 0 \\ \Rightarrow 2x^2 + 22x - 204 &= 0 \\ \Rightarrow x^2 + 11x - 102 &= 0 \\ \Rightarrow x^2 + 17x - 6x - 102 &= 0 \\ \Rightarrow x(x+17) - 6(x+17) &= 0 \\ \Rightarrow (x-6)(x+17) &= 0 \\ \Rightarrow x &= 6 \text{ as } x \neq -17 \end{aligned}$$

42. (b)



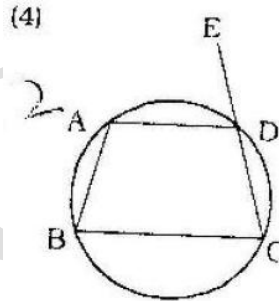
$$\begin{aligned} \angle ABC + \angle CDA &= 180^\circ \\ \therefore \angle CDA &= 180^\circ - 70^\circ = 110^\circ \\ \therefore \angle BCD &= 180^\circ - 110^\circ = 70^\circ \end{aligned}$$

43. (c)



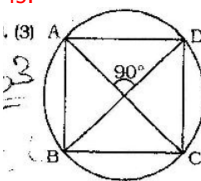
$$\begin{aligned} \angle ABC + \angle ADC &= 180^\circ \\ \angle CBE &= 50^\circ \\ \therefore \angle ABC &= 180^\circ - 50^\circ = 130^\circ \\ \therefore \angle ADC &= 180^\circ - 130^\circ = 50^\circ \end{aligned}$$

44. (d)



$$\begin{aligned} \angle ABC + \angle CDA &= 180^\circ \\ \Rightarrow \angle CDA &= 180^\circ - 72^\circ = 108^\circ \\ AD &\parallel BC \\ \angle BCD &= \angle ADE = \angle ABC = 72^\circ \end{aligned}$$

45. (3)



$$\begin{aligned} \angle B + \angle D &= 180^\circ \\ \angle A + \angle C &= 180^\circ \\ \angle BAC &= \angle BCA \\ \angle DAC &= \angle DCA \\ \therefore \angle DAB &= \angle DCB = 90^\circ \\ \angle DAC &= \theta \\ \therefore \angle ADE &= 90^\circ - \theta = \angle CDE \\ \therefore \angle ABC &= 180^\circ - 2(90^\circ - \theta) \\ &= 180^\circ - 180^\circ + 2\theta = 2\theta \end{aligned}$$